

# **Intelligent Anti-Money Laundering Solution Based upon Novel Community Detection in Massive Transaction Networks on Spark**

**2017**

# Introduction

- AML system: rule-based, lack of pattern recognition function
- Divide complex structures into meaningful subgroups and calculate the suspicious degree for each group
- **Temporal-directed Louvain algorithm**
- Implement on Spark GraphX platform

# Design and implementation

- A. Select effective maximal connected subgraph in massive transaction networks
- B. Community detection according to ML characteristics
  - Edge weight optimization by node correction
  - Temporal correction for edge weight
  - Directed optimization for modularity
- C. Money laundering risk quantization for Communities

## A. Select effective maximal connected subgraph in massive transaction networks

- Focus on the transaction data in a certain time period  $P_t$
- Node: account, edge: transfer
- Merge the edge between node pairs with the same source and destination
  - $w_{Bi} = e^{\omega_m \cdot M_i + \omega_c \cdot C_i}$ , where  $\omega_m + \omega_c = 1$
- Divide the graph into different maximal connected subgraphs (MCS)
  - Filter the MCSs by the formula:  $V_{\theta 1} < V_{mcs} < V_{\theta 2}$
- Hub nodes: the node whose degree exceeds a threshold  $D_\theta$ 
  - MCSs can be further filtered by  $N_{hubs} > N_\theta$

## B. Community detection according to ML characteristics

### A) Edge weight optimization by node correction

- Louvain algorithm: overlook the weight of node -> need corrections
- The suspicious degree of a node is also important
- Node correction for *src*:  $\sigma_s = e^{\omega_{Mv} \cdot M_s + \omega_{Cv} \cdot C_s + \omega_{Dv} \cdot D_s}$
- Node correction for *dst*:  $\sigma_d = e^{\omega_{Mv} \cdot M_d + \omega_{Cv} \cdot C_d + \omega_{Dv} \cdot D_d}$
- New edge weight:  $W_{Ni} = \sigma_s * \sigma_d * W_{Bi}$

## B. Community detection according to ML characteristics

### B) Temporal correction for edge weight

- $t_A^{in}$  and  $t_A^{out}$  : node's average time point of all inbound and outbound transfers
- $T_{s \rightarrow d}$  : average transfer time point for edge  $src \rightarrow dst$
- $Deg_s^{in}$  and  $Deg_s^{out}$  : the number of all inbound and outbound transfers for  $src$

## B. Community detection according to ML characteristics

### B) Temporal correction for edge weight

Pattern 1: “Centralized out after multi-transfer in” (for edge  $src \rightarrow dst$ )

- $Deg_s^{in} > Deg_s^{out}$  and  $T_{s \rightarrow d} > t_s^{in}$  : promote edge weight
- $Deg_s^{in} > Deg_s^{out}$  but  $T_{s \rightarrow d} < t_s^{in}$  : reduce edge weight
- The correction factor  $\theta_s = e^{\beta_s \cdot \tau_s^{out}}$   
, where  $\beta_s = \frac{Deg_s^{in} - Deg_s^{out}}{Deg_s^{in} + Deg_s^{out}}$ ,  $\tau_s^{out} = \frac{P_T}{(T_{s \rightarrow d} - t_s^{in})}$
- $\theta_s > 1$  if  $Deg_s^{in} > Deg_s^{out}$  and  $T_{s \rightarrow d} > t_s^{in}$ , else  $\theta_s \leq 1$

## B. Community detection according to ML characteristics

B) Temporal correction for edge weight

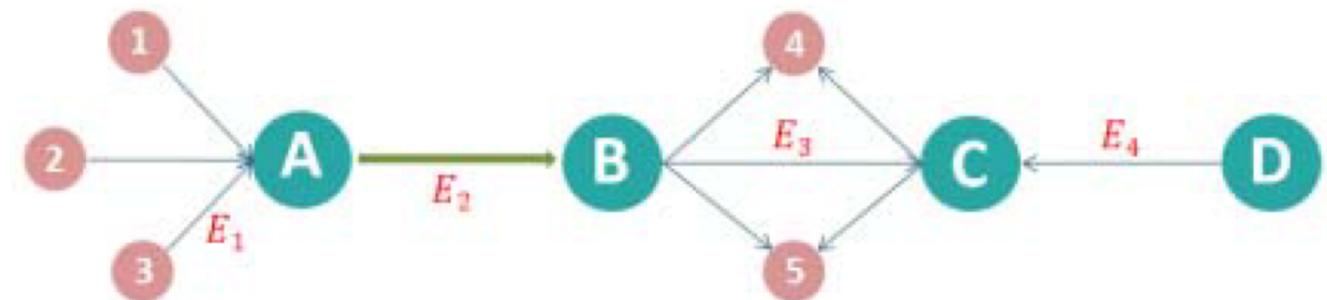
Pattern 2: “centralized in edge before multi-transfer out” (for destination node)

- $Deg_d^{int} < Deg_d^{out}$  and  $T_{s \rightarrow d} < t_d^{out}$

- The correction factor  $\theta_d = e^{\beta_d \cdot \tau_d^{in}}$

, where  $\beta_d = \frac{Deg_d^{in} - Deg_d^{out}}{Deg_d^{in} + Deg_d^{out}}$ ,  $\tau_d^{in} = \frac{P_T}{(T_{s \rightarrow d} - t_d^{out})}$

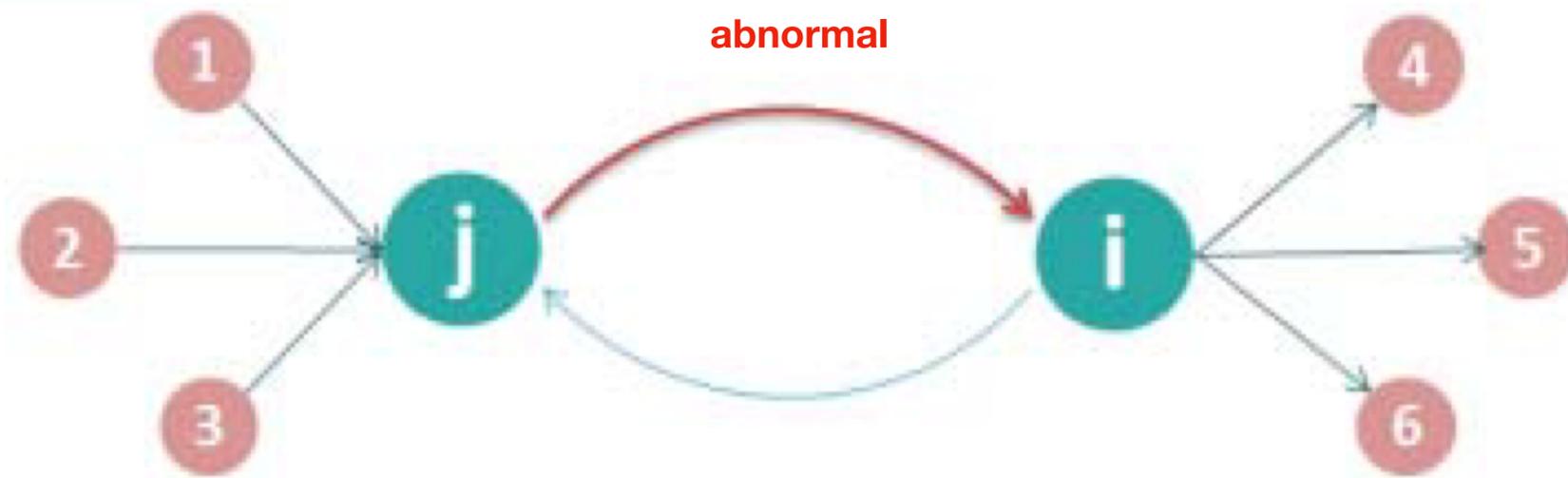
- $$W_{Ei} = \begin{cases} \theta_s \cdot \theta_d \cdot W_{Ni}, & \beta_s > 0 \text{ and } \beta_d < 0 \\ \theta_s \cdot W_{Ni}, & \beta_s > 0 \text{ and } \beta_d > 0 \\ \theta_d \cdot W_{Ni}, & \beta_s < 0 \text{ and } \beta_d < 0 \\ W_{Ni}, & \beta_s < 0 \text{ and } \beta_d > 0 \end{cases}$$



## B. Community detection according to ML characteristics

### C) Directed optimization for modularity

- Consider the asymmetry of information caused by the direction of edges
- Example:
  - Node  $i$  : low in-degree, high out-degree
  - Node  $j$  : high in-degree, low out-degree



## B. Community detection according to ML characteristics

### C) Directed optimization for modularity

- Revision for Louvain algorithm:

$$Q = \frac{1}{2m} \sum_{ij} \left[ A_{ij} - \frac{k_i k_j}{2m} \right] \delta(c_i, c_j),$$

- Define  $k_n^{in}$ ,  $k_n^{out}$ ,  $k_n$  is the sum of edge weight linked in, out, and with node
- Revised factor  $\delta_n = (k_n^{in} - k_n^{out}) / k_n$

$$Q_D = \frac{1}{2m} \sum_{i,j} \left[ A_{ij} - \frac{e^{\delta_i - \delta_j} k_i k_j}{2m} \right] \delta(c_i, c_j)$$

$$= \frac{1}{2m} \left[ \sum_{i,j} A_{ij} - \frac{\sum_i e^{\delta_i} k_i \sum_j e^{-\delta_j} k_j}{2m} \right] \delta(c_i, c_j) = \sum_c \left[ \frac{\sum W_{ec}}{2m} - \left( \frac{1}{2m} \right)^2 \sum M_c \right]$$

## B. Community detection according to ML characteristics

\* Louvain algorithm:

- Modularity: measures the relative density of edges inside communities with respect to edges outside communities

$$Q = \frac{1}{2m} \sum_{ij} \left[ A_{ij} - \frac{k_i k_j}{2m} \right] \delta(c_i, c_j),$$

- Compare to a randomly rewired network

- Divide an edge into 2 stubs -> m edges become 2m stubs

- The probability for a stub of node  $i$  connecting with node  $j$ :  $\frac{k_j}{2m - 1}$

- The probability for node  $i$  connecting with node  $j$ :  $\frac{k_i k_j}{2m - 1}$

## B. Community detection according to ML characteristics

- $A_{ij}$  is the weight of the edge between  $i$  and  $j$
- $m = \frac{1}{2} \sum_{i,j} A_{ij}$  is the sum of edge weights in the whole graph.
- $\delta(c_i, c_j) = 1$  if  $c_i = c_j$ , else  $\delta(c_i, c_j) = 0$
- $c_i$  is the community where node  $i$  belongs to
- $k_i$  is the sum of all edge weights attached to node  $i$
- $M_c$  is the corresponding matrix for each community
- $\sum M_c$  is the sum of all elements in  $M_c$
- $\sum_c$  means accumulating in the original community

$$M_c = \begin{bmatrix} e^{\delta_1 - \delta_1} k_1 k_1, & e^{\delta_1 - \delta_2} k_1 k_2, & \dots & e^{\delta_1 - \delta_N} k_1 k_N \\ e^{\delta_2 - \delta_1} k_2 k_1, & e^{\delta_2 - \delta_2} k_2 k_2, & \dots & e^{\delta_2 - \delta_N} k_2 k_N \\ \vdots & \vdots & \ddots & \vdots \\ e^{\delta_N - \delta_1} k_N k_1, & e^{\delta_N - \delta_2} k_N k_2, & \dots & e^{\delta_N - \delta_N} k_N k_N \end{bmatrix}$$

## B. Community detection according to ML characteristics

- Temporal-directed Louvain algorithm:

Step 1: Initialize the community tag for each node by using its own node tag.

Step 2: For each node, maximize the difference  $\Delta Q_D$  between allocating it in the original community and the neighbor community  $\rightarrow$  if the maximum  $\Delta Q_D > 0$ , actualize the allocation. Following is the revised formula for  $\Delta Q_D$

$$\Delta Q_D = \left[ \frac{\sum W_{ec} + k_i^c}{2m} - \frac{1}{(2m)^2} \sum M_{c_{new}} \right] - \left[ \frac{\sum W_{ec}}{2m} - \frac{1}{(2m)^2} \sum M_c - \frac{e^{\delta_i - \delta_i} k_i k_i}{(2m)^2} \right] = \frac{k_i^c}{2m} - \frac{\sum M_{c_{new}} - \sum M_c - k_i k_i}{(2m)^2} = \frac{k_i^c}{2m} - \frac{\Theta_i}{(2m)^2} \quad (4)$$

- $k_i^c$ : the total weight of edges formed between node  $i$  and all nodes in the community

$$\Theta_i = k_i e^{\delta_i} \sum_c k_j e^{-\delta_j} + k_i e^{-\delta_i} \sum_c k_j e^{\delta_j} \quad M_{c_{new}} = \begin{bmatrix} e^{\delta_1 - \delta_1} k_1 k_1, & e^{\delta_1 - \delta_2} k_1 k_2, & \dots & e^{\delta_1 - \delta_N} k_1 k_N, & e^{\delta_1 - \delta_i} k_1 k_i \\ e^{\delta_2 - \delta_1} k_2 k_1, & e^{\delta_2 - \delta_2} k_2 k_2, & \dots & e^{\delta_2 - \delta_N} k_2 k_N, & e^{\delta_2 - \delta_i} k_2 k_i \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ e^{\delta_N - \delta_1} k_N k_1, & e^{\delta_N - \delta_2} k_N k_2, & \dots & e^{\delta_N - \delta_N} k_N k_N, & e^{\delta_N - \delta_i} k_N k_i \\ e^{\delta_i - \delta_1} k_i k_1, & e^{\delta_i - \delta_2} k_i k_2, & \dots & e^{\delta_i - \delta_N} k_i k_N, & e^{\delta_i - \delta_i} k_i k_i \end{bmatrix}$$

## **B. Community detection according to ML characteristics**

- Temporal-directed Louvain algorithm:

Step 3: Repeat Step 2 until the community tag of all nodes does not change.

Step 4: Compress nodes with the same community label into a new node.

Original total edge weight  $\rightarrow$  self-link weight of new node

Step 5: Repeat Step 2 until the modularity of the whole graph does not change

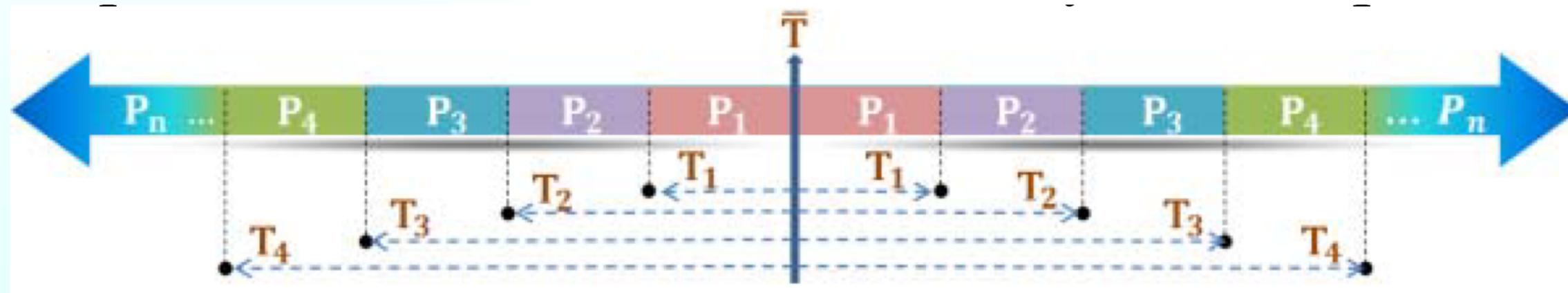
## C. Money laundering risk quantization for Communities

- ML risk score for the community  $k$ :  $\Psi_k = e^{w_k \cdot V_k + w_E \cdot E_k + w_M \cdot M_k + w_D \cdot D_k + w_H \cdot H_k}$
- $V_k$  : total nodes number
- $E_k$  : total edge number
- $M_k$  : total money amount
- $D_k$  : average node suspicious degree
- Temporal entropy  $H_c = - \sum_{i=1}^n P_i * \log_2 P_i$   
(to measure the transfer time concentration)

## C. Money laundering risk quantization for Communities

- $\bar{T}$  : the average time point of a community
- $\Delta T$  : the absolute interval between each transfer time point and  $\bar{T}$
- $P_1$  is the percentage of transactions in the segment of  $0 \leq \Delta T \leq T_1$
- $P_2$  is the percentage of transactions in the segment of  $T_1 \leq \Delta T \leq T_2 \dots$

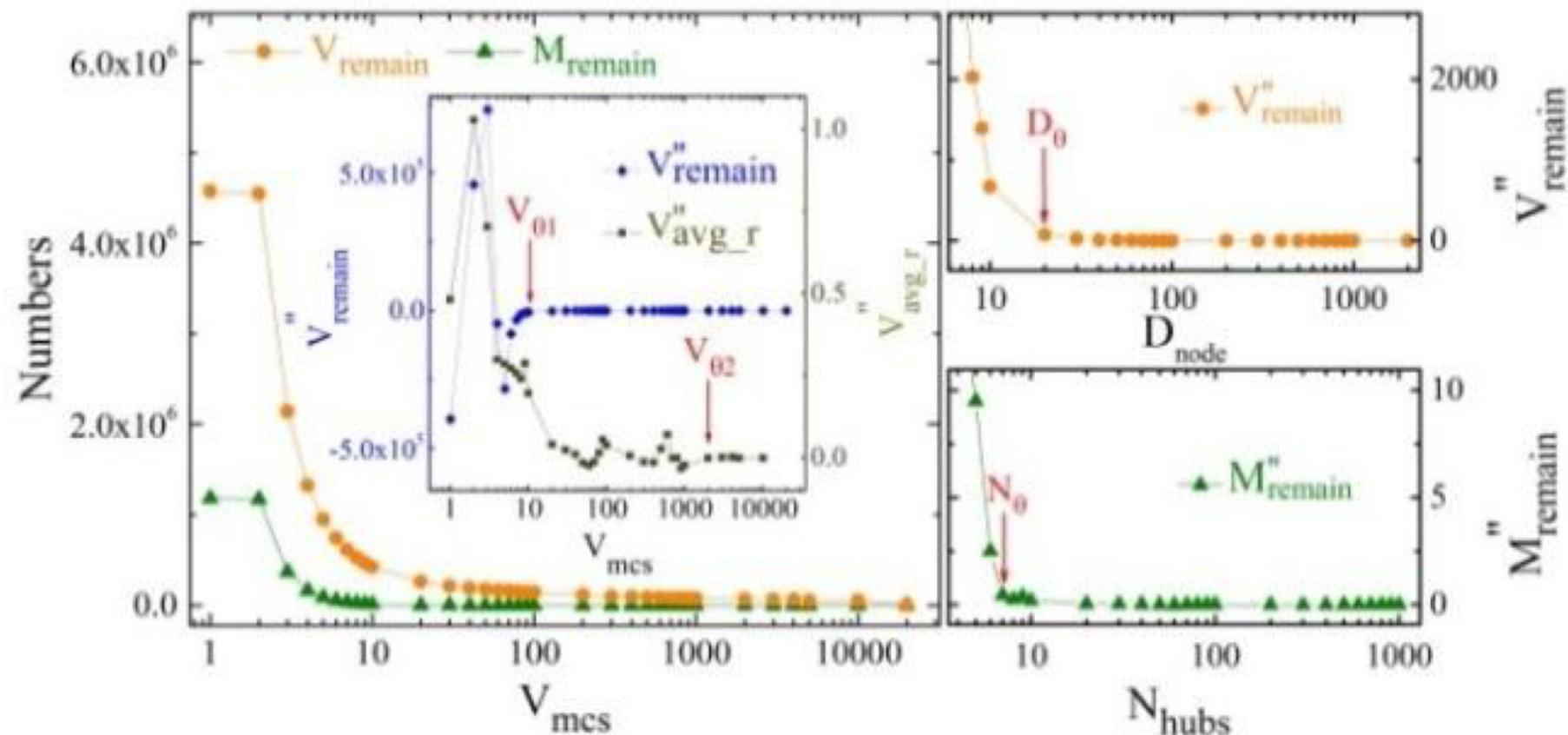
- All segments should obey  $\sum_{i=1}^n P_i = 1$



# **III. EXPERIMENTS AND RESULTS**

## A. Determination of Filter's Parameter

- Data: around 10 million of real transfer records in the first week of November 2016 -> filtered -> scale down to 45% of original size
- Filter's Parameter:  $V_{\theta 1}$  ,  $V_{\theta 2}$  ,  $D_{\theta}$  ,  $N_{\theta}$
- $V_{avg_r} = V_{remain} / M_{remain}$



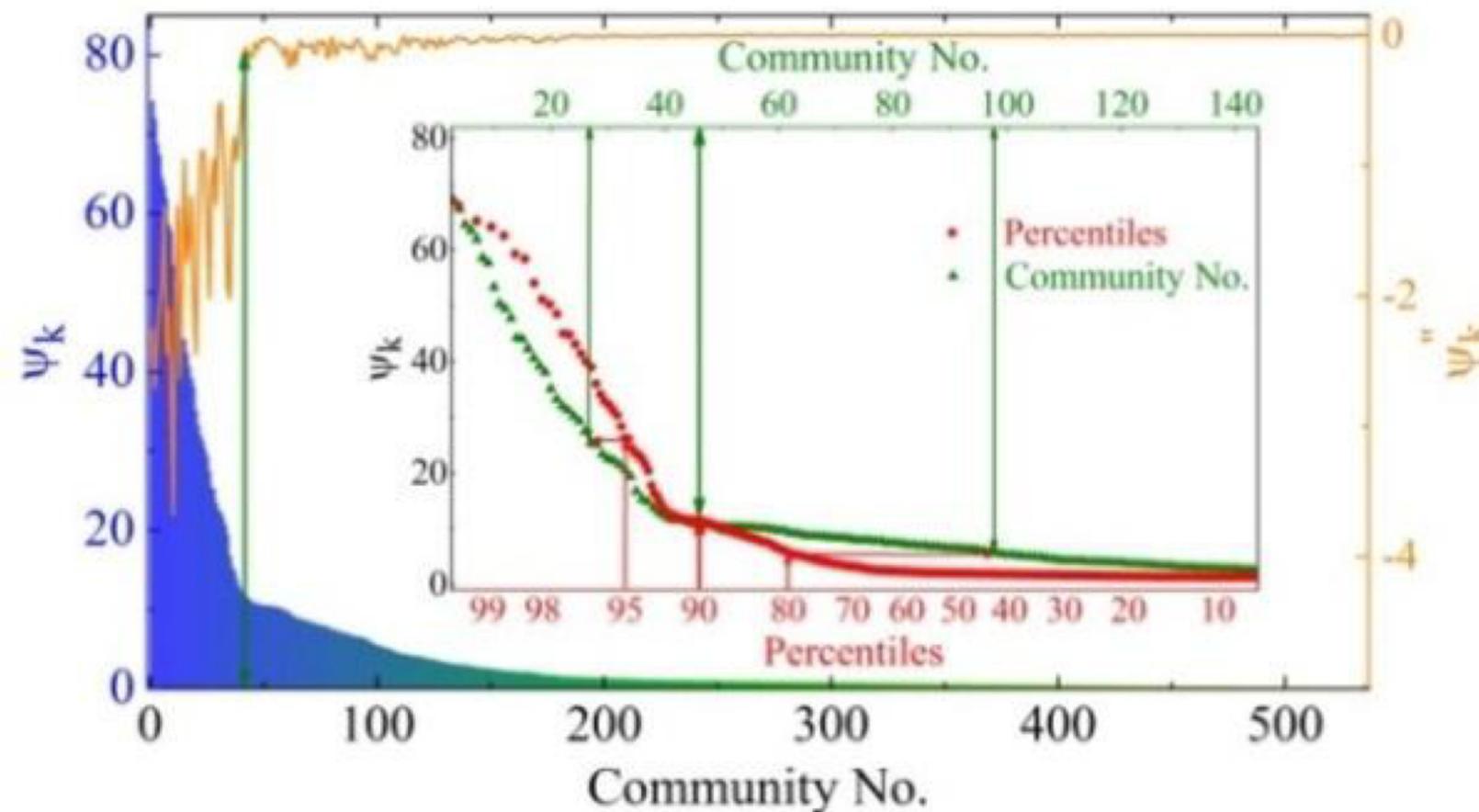
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Recall

## B. ML risk level partition

- Orange line: first derivative for the risk score
- 95% ~ 100%: level 1, 90% ~ 95%: level 2, 80% ~ 90%: level 3
- After reporting level 1, 2 -> 9/13 were reconfirmed suspicious



## C. TD Louvain algorithm v.s. Louvain algorithm

- Nodes ascribed to different communities are drawn in distinct colors
- Edges are also drawn in progressive color with increasing time

